

The function $f(x)$ is defined on the interval $[0, 2\pi]$. The function $f(x)$ is continuous on $[0, 2\pi]$ and has a jump discontinuity at $x = \pi$. The function $f(x)$ is defined by

$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{for } 0 < x < \pi \\ \pi - x & \text{for } \pi < x < 2\pi \end{cases}$$

The function $f(x)$ is continuous on $[0, \pi)$ and $(\pi, 2\pi]$. The function $f(x)$ has a jump discontinuity at $x = \pi$. The function $f(x)$ is defined by

$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{for } 0 < x < \pi \\ \pi - x & \text{for } \pi < x < 2\pi \end{cases}$$

$$C_{k;k;l}^{j;j';m} = \int_{-\infty}^{+\infty} J_k(x) J_{k'}(x) I_l(x) dx M$$

The function $J_k(x)$ is the Bessel function of the first kind of order k . The function $J_{k'}(x)$ is the Bessel function of the first kind of order k' . The function $I_l(x)$ is the modified Bessel function of the first kind of order l . The function M is the measure. The function $C_{k;k;l}^{j;j';m}$ does not depend on the order of the coefficients k, k', l and j, j', m . The function $C_{k;k;l}^{j;j';m}$ is defined on N_s and is continuous on N_s . The function $C_{k;k;l}^{j;j';m}$ is defined on N_s and is continuous on N_s . The function $C_{k;k;l}^{j;j';m}$ is defined on N_s and is continuous on N_s .

II Multiresolution algorithm for evaluating u

Let $\{V_j\}_{j \in \mathbb{Z}}$ be a multiresolution analysis of $L^2(\mathbb{R})$ with scaling function ϕ and wavelet functions ψ_k .

Let $f \in L^2(\mathbb{R})$ and let $\{c_j\}_{j \in \mathbb{Z}}$ be the coefficients of the expansion of f in the multiresolution analysis $\{V_j\}_{j \in \mathbb{Z}}$.

$$f = \sum_{j \in \mathbb{Z}} c_j \phi_j$$

The multiresolution algorithm for evaluating u consists of computing the coefficients c_j of the expansion of f in the multiresolution analysis $\{V_j\}_{j \in \mathbb{Z}}$.

$$\|f\|_0^2 = \sum_{j=1}^n [\|c_{j-1}\|_0^2 + \|c_j\|_0^2] = \sum_{j=1}^n \|c_{j-1}\|_0^2 + \|c_n\|_0^2$$

Let $\{c_j\}_{j=1}^n$ be the coefficients of the expansion of f in the multiresolution analysis $\{V_j\}_{j=1}^n$.

$$\|f\|_0^2 = \sum_{j=1}^n \|c_j\|_0^2 = \|c_n\|_0^2$$

o

$$\sum_{j=1}^n \|c_j\|_0^2$$

→ $o(u^2)$ ss

Le y considère n

$$\left\{ \begin{matrix} 1 \\ k \end{matrix} \right\} \rightarrow \left\{ \begin{matrix} 2 \\ k \end{matrix} \right\} \rightarrow \left\{ \begin{matrix} 2 \\ k \end{matrix} \right\} \rightarrow \left\{ \begin{matrix} 3 \\ k \end{matrix} \right\} \rightarrow \left\{ \begin{matrix} 3 \\ k \end{matrix} \right\} \rightarrow \left\{ \begin{matrix} 3 \\ k \end{matrix} \right\} \dots$$

$$\searrow \qquad \qquad \qquad \searrow \qquad \qquad \qquad \searrow$$

$$\{d_k^2\} \rightarrow \{d_k^2\} \rightarrow \{d_k^2\} \rightarrow \{d_k^3\} \rightarrow \{d_k^3\} \rightarrow \{d_k^3\} \dots$$

e fo e co e ed e ence nd e e s d_k^{j+1} nd k^{j+1} e en dd k^{j+1}

$$\sum_{j=1}^n \sum_{k \in \mathbb{Z}} d_k^j \quad d_k^j \quad k^j \quad \sum_{k \in \mathbb{Z}} \binom{n}{k} \binom{n}{k} \binom{n}{k} \binom{n}{k}$$

ce e en e of o e on s fo co n e e n on of 2
 o o on o en e of s n c n co e c e n s d_k n e e e n on of o
 n e o s c e f e o n f n c o n s e e n e d y e c o of e e n N e n
 e n e of o e on s s o o on o N f e o n f n c o n s e e n e d
 y o_2 N s n c n c o e c e n s e n e n e of o e on s o co e s
 s e s o o on o o_2 N e o n n d s e s y e n e z e o
 e n d n s o n c e

o n u^2 n s s

e no e n o e e n e c e of e e s n d e e n o e e n d
 n o e e e s n e n e c e of e e s e o d c o n e n
 s e s o e n o e f n e s e s n d e d e o n e c e n o o o n d e
 s o e e e c o c y s o o e d e e s o o o c o n d e o n s e n o
 e s c e d o s e e s e d e n o e e s n f n c o n y n d e e e y
 e e e s s e n e n y k^{j-2} - j - M \in \mathbb{Z} e e e
 c o n d e e e o n n y s s o c e d e s s
 n o d e o e n d e e n n o e e e s e e e d o c o n d e
 e n e s o f e o d c o f e s f n c o n s f o e e

$$M_{www}^{jj'} M' M \int_{-\infty}^{+\infty} \binom{j}{k} \binom{j}{k'} \binom{j'}{l} d M$$

e e' \leq \quad s c e e e c o e c e n s M_{www}^{jj'} M' M e d e n f c y z e o f o
 | - ' | > 0 e e o d e p e n d s o n e o e o f e s o f e s f n c o n s
 e n e of n e c e s s y c o e c e n s y e e d c e d f e y o s n e

$$M_{www}^{jj'} M' M^{-j'-2} \int_{-\infty}^{+\infty} \binom{j-j'}{0} \binom{j-j'}{k-k'} \binom{0}{2j-j'-k-l} d M$$

o M_0 M_1 M_2 M_3 M_4 M_5 M_6 M_7 M_8 M_9 M_{10} M_{11} M_{12} M_{13} M_{14} M_{15} M_{16} M_{17} M_{18} M_{19} M_{20} M_{21} M_{22} M_{23} M_{24} M_{25} M_{26} M_{27} M_{28} M_{29} M_{30} M_{31} M_{32} M_{33} M_{34} M_{35} M_{36} M_{37} M_{38} M_{39} M_{40} M_{41} M_{42} M_{43} M_{44} M_{45} M_{46} M_{47} M_{48} M_{49} M_{50} M_{51} M_{52} M_{53} M_{54} M_{55} M_{56} M_{57} M_{58} M_{59} M_{60} M_{61} M_{62} M_{63} M_{64} M_{65} M_{66} M_{67} M_{68} M_{69} M_{70} M_{71} M_{72} M_{73} M_{74} M_{75} M_{76} M_{77} M_{78} M_{79} M_{80} M_{81} M_{82} M_{83} M_{84} M_{85} M_{86} M_{87} M_{88} M_{89} M_{90} M_{91} M_{92} M_{93} M_{94} M_{95} M_{96} M_{97} M_{98} M_{99}

need of \mathbb{R}^n can be considered in

$$\mathbf{V}_0 \times \mathbf{V}_0 \rightarrow \mathbf{V}_0$$

for any $\mathbf{v} \in \mathbf{V}_0$

$$\sum_k \mathbf{v}_k = M$$

the set of linear equations $\mathbf{v}_k = \mathbf{v}_k$ and $\mathbf{v}_k = \mathbf{v}_k$

References

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